# Uninformed Search Lecture 4

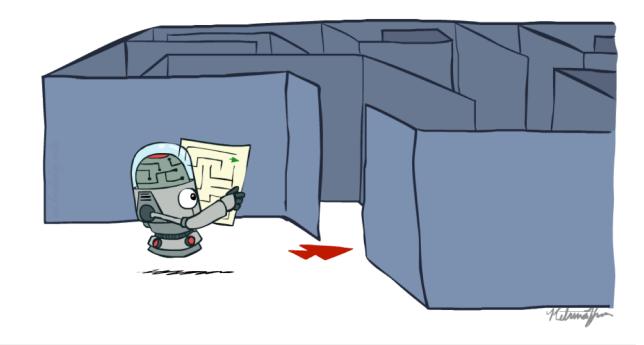
What are common search strategies that operate only given the search problem formalism? How do they compare?



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# Agenda

- A quick refresher
- DFS, BFS, ID-DFS, UCS
- Unification!



## Search Problem Formalism

Defined via the following components:

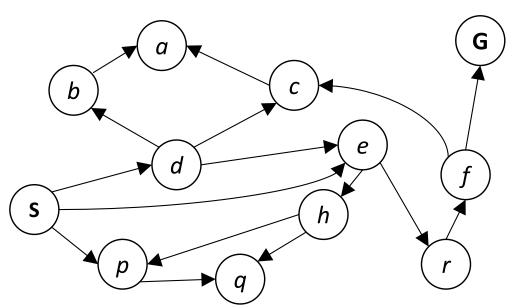
- The initial state the agent starts in
- A successor/transition function
  - $S(x) = \{action + cost state\}$
- A goal test, which determines whether a given state is a goal state
- A path cost that assigns a numeric cost to each path

A **solution** is a sequence of actions leading from initial state to a goal state. (**Optimal** = lowest path cost.)

Together the initial state and successor function implicitly define the **state space**, the set of all reachable states

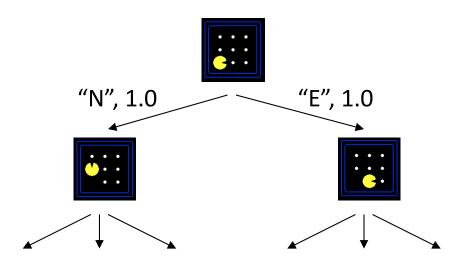
# State Space Graph

- State space graph: A mathematical representation of a search problem
  - Nodes are (abstracted) world configurations
  - Arcs represent successors (action results)
  - The goal test is a set of goal node(s)
- In a search graph, each state occurs only once!
- We can rarely build this full graph in memory (it's too big), but it's a useful idea



## Search Tree

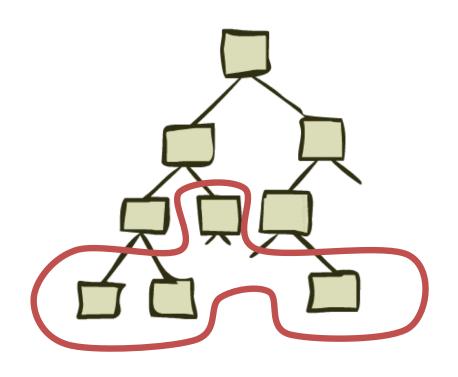
- A "what if" tree of plans and their outcomes
- The start state is the root node
- Children correspond to successors
- Nodes show states, but correspond to PLANS that achieve those states
- For most problems, we can never actually build the whole tree



# Searching for Solutions

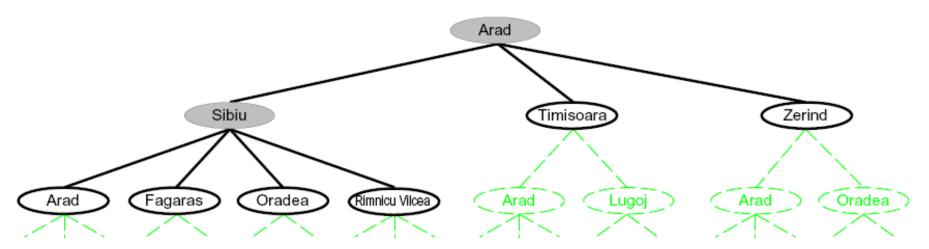
Basic idea: incrementally build a search tree until a goal state is found

- Root = initial state
- Expand via transition function to create new nodes
- Nodes that haven't been expanded are leaf nodes and form the frontier (open list)
- Different search strategies (next lecture) choose next node to expand (as few as possible!)
- Use a closed list to prevent expanding the same state more than once



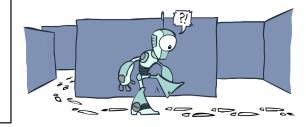


# General Algorithm



```
function GRAPH-SEARCH(problem, fringe) returns a solution, or failure  \begin{array}{l} closed \leftarrow \text{an empty set} \\ fringe \leftarrow \text{INSERT}(\text{MAKE-NODE}(\text{INITIAL-STATE}[problem]), fringe) \\ \textbf{loop do} \\ \textbf{if } fringe \text{ is empty then return failure} \\ node \leftarrow \text{REMOVE-FRONT}(fringe) \\ \textbf{if } \text{GOAL-TEST}(problem, \text{STATE}[node]) \textbf{ then return } node \\ \textbf{if } \text{STATE}[node] \text{ is not in } closed \textbf{ then} \\ \textbf{add } \text{STATE}[node] \text{ to } closed \\ fringe \leftarrow \text{INSERTALL}(\text{EXPAND}(node, problem), fringe) \\ \textbf{end} \end{array}
```

Queue (FIFO) Stack (LIFO) Priority Queue





**Uninformed Search** 

# Evaluating a Search Strategy

#### **Solution**

- Completeness: does it always find a solution if one exists?
- Optimality: does it always find a least-cost solution?

#### **Efficiency**

- Time Complexity: number of nodes generated/expanded
- Space Complexity: maximum number of nodes in memory

# Depth-First Search (DFS)



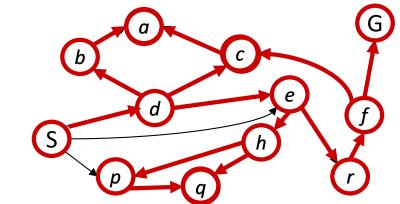


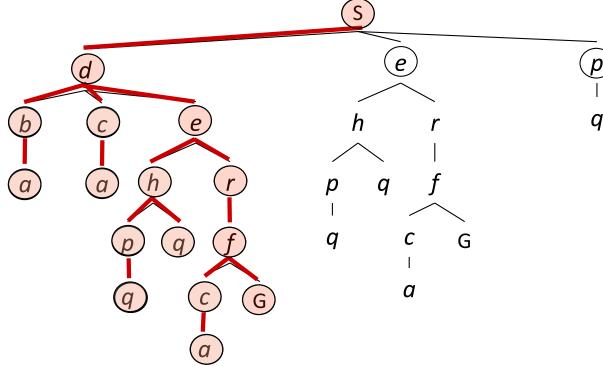
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# DFS Example

Strategy: expand a deepest node first

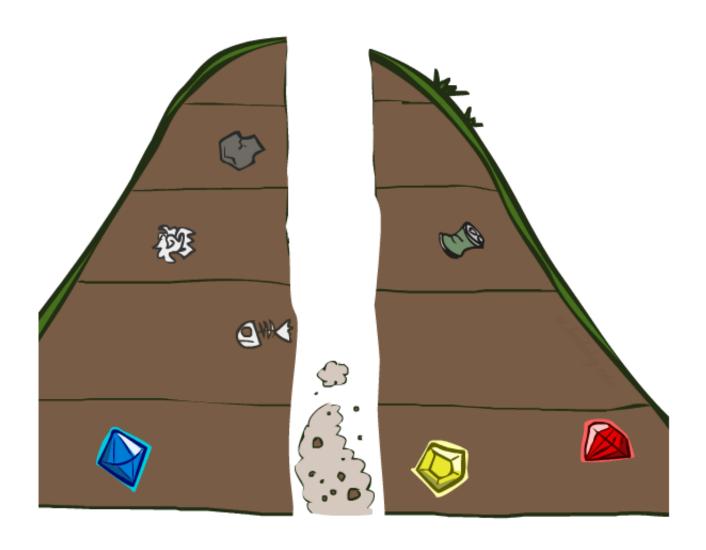
Implementation: Fringe is a LIFO stack







## Let's Evaluate!

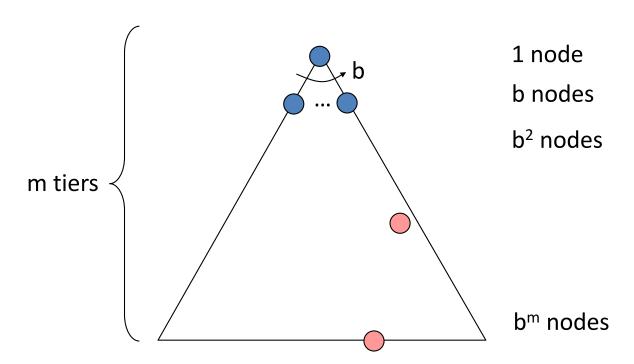




## Search Tree

## **Properties**

- Branching factor
- Maximum depth
- Solutions at various depths



Number of nodes in the tree?

•  $1 + b + b^2 + \dots b^m = O(b^m)$ 

## DFS Evaluation

#### Time

- Expands left
  - Could be whole tree!
- Assuming finite depth,  $O(b^m)$

# 1 node m tiers b<sup>m</sup> nodes

b nodes

b<sup>2</sup> nodes

#### **Space**

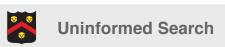
Only siblings on path, O(bm)

#### **Complete**

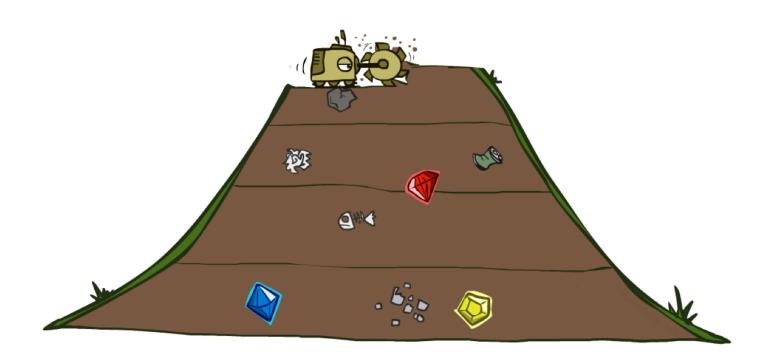
Only if finite

#### **Optimal**

No, "left-most" w/o regard to cost/depth



# Breadth-First Search (BFS)

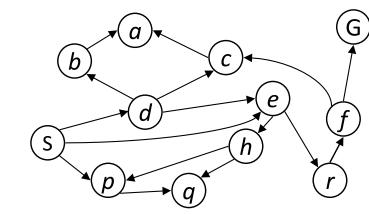


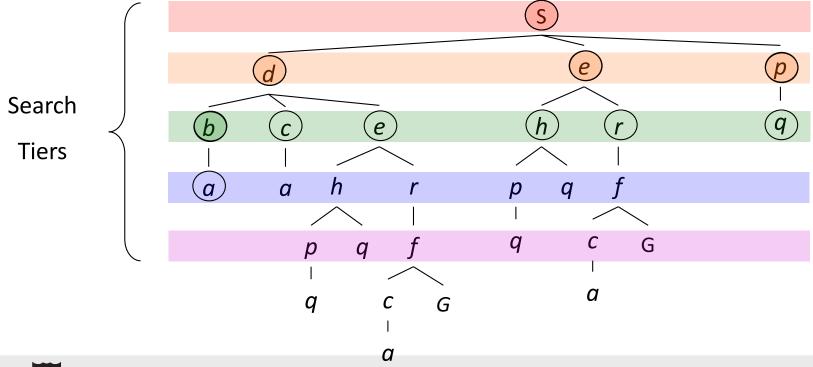
# BFS Example

Strategy: expand a shallowest node first

*Implementation: Fringe* 

is a FIFO queue



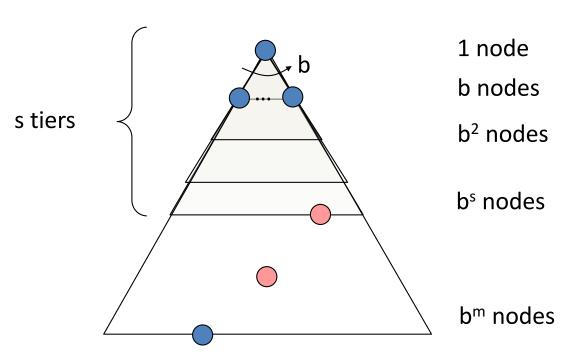




## **BFS** Evaluation

#### **Time**

 Processes all nodes above shallowest solution, O(b<sup>s</sup>)



#### **Space**

 Has roughly the last tier, so O(b<sup>s</sup>)

#### <u>Complete</u>

Yes!

#### **Optimal**

 Only if all costs equal (more later)



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## DFS vs. BFS



Empty-BFS

Maze-DFS

Maze-BFS

# Grounding the Branching Factor

Depth	Nodes	Time	Memory
2	110	0.11 msecs	107 KB
4	11,110	11 msecs	10.6 MB
6	<b>10</b> <sup>6</sup>	1.1 secs	1 GB
8	108	2 mins	103 GB
10	10 <sup>10</sup>	3 hours	10 TB
12	10 <sup>12</sup>	13 days	1 PB
14	1014	3.5 years	99 PB
16	<b>10</b> <sup>16</sup>	350 years	10 EB

#### **Assumptions**

- b = 10
- 1 million nodes/second
- 1000 bytes/node

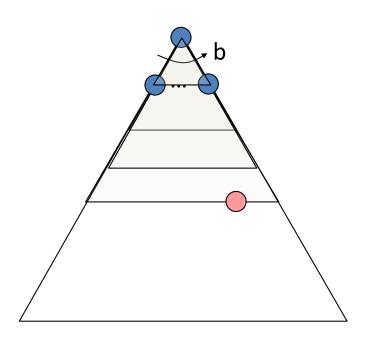
Memory often becomes the limiting factor



# **Iterative Deepening DFS**

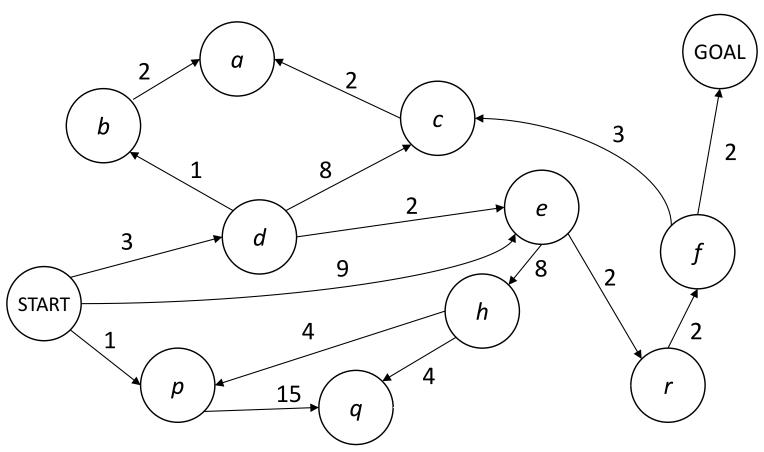
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- Basic idea: DFS memory with BFS time/shallow solution
  - DFS up to 1
  - DFS up to 2
  - **—** ....
- Generally most work happens in the lowest level searched, so not too wasteful



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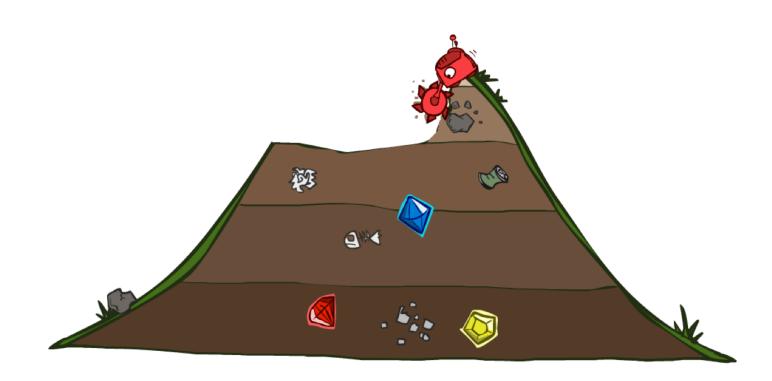
## Cost-Sensitive Search

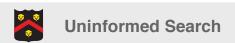


- BFS finds the shortest path in terms of number of actions, but it does not find the least-cost path.
- We will now cover a similar algorithm which does!



# Uniform-Cost Search (UCS)



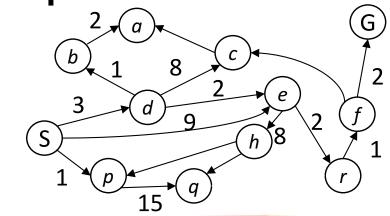


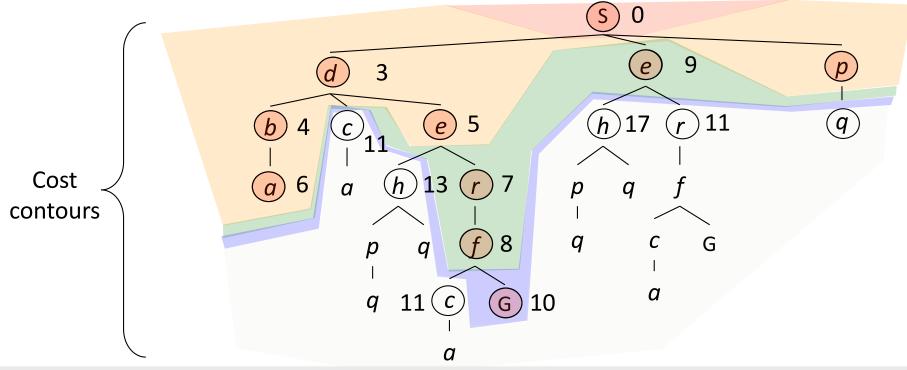
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## **UCS** Example

Strategy: expand a cheapest node first

Fringe is a priority queue (priority: cumulative cost)







## **UCS** Evaluation

## <u>Time</u>

O(b<sup>C\*/ε</sup>)

## **Space**

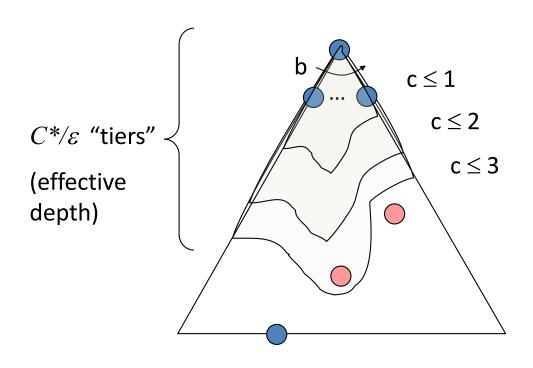
O(b<sup>C\*/ε</sup>)

### **Complete**

Yes!

### <u>Optimal</u>

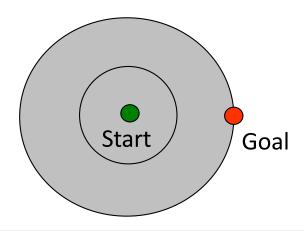
Yes!

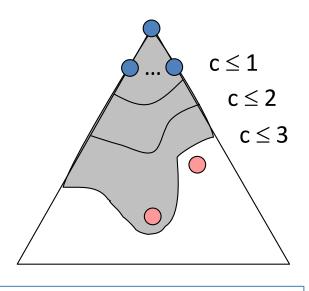


Assume solution costs C\* and arcs cost at least  $\varepsilon$ 

## UCS vs. DFS vs. BFS

- UCS is good and optimal
- However, it still moves in every direction – it's not informed about goal direction...



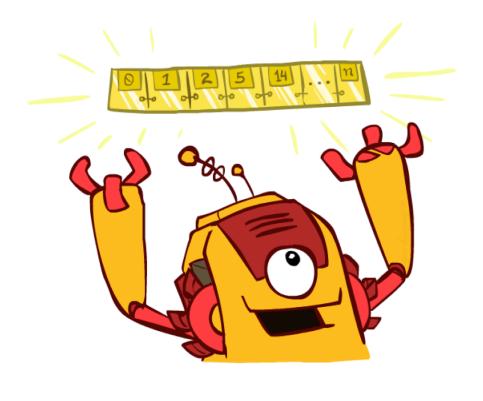


- Empty-UCS
- Maze-UCS
- MazeCost-DFS
- MazeCost-BFS
- MazeCost-UCS



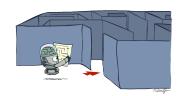
## Unification

- All these search algorithms are the same except for fringe strategies
- Conceptually, all fringes are priority queues (i.e. collections of nodes with attached priorities)
- Practically, for DFS and BFS, you can avoid the log(n) overhead from an actual priority queue, by using stacks and queues



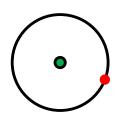
## **Uninformed Search**

## Search given only the problem definition



	DFS	BFS	UCS
Fringe	LIFO (stack)	FIFO (queue)	PQ (path cost)
Complete		X	X
Optimal			X
Time	$\mathcal{O}(b^m)$	$\mathcal{O}(b^s)$	$\mathcal{O}(b^{\mathcal{C}^*/arepsilon})$
Space	$\mathcal{O}(bm)$	$\mathcal{O}(b^s)$	$\mathcal{O}(b^{\mathcal{C}^*/arepsilon})$

Assumptions: potentially infinite depth, arbitrary positive action costs







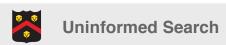


## **A Reminder**

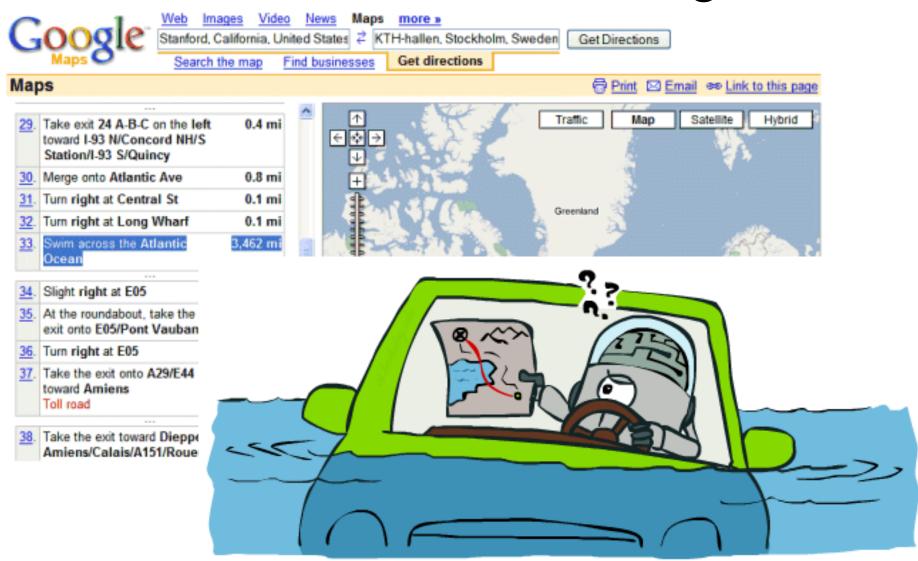
- Search operates over models of the world
- The agent doesn't actually try all the plans out in the real world!
- Planning is all "in simulation"



 Your search is only as good as your models...



# Search Gone Wrong





# Summary

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- We evaluated several uninformed strategies to solve a search problem
  - DFS, ID-DFS, BFS, UCS

 DFS, BFS, and UCS can all be implemented via a generic graph-search algorithm over a search tree by simply changing how the fringe is organized