

EECS 280

Discussion #3

Week of January 21

Outline

- * Administrivia
- * Tail Recursion
- * Function Pointers

Announcements

- * Assignment #2
- * Due January 31st @ 11:59 PM
- * Discussion Slides
- * My slides will be available online before discussion, official notes to follow on CTools
- * <http://www-personal.umich.edu/~nlderbin/eecs280>

Outline

- * Administrivia
- * Tail Recursion
- * Function Pointers

Recursion Review

- * Style of programming whereby a function calls itself
- * Usually consists of components
 - * Base Case(s): small case solution
 - * Pre-processing: large case -> small case
 - * Recursive Call(s): process small case
 - * Post-processing: process small case solution

Recursion Breakdown

```
int factorial( int n )
{
    if ( n == 0 )
        return 1;
    else
        return ( n * factorial( n-1 ) );
}
```

Recursion Breakdown

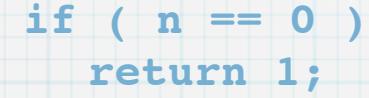
```
int factorial( int n )
{
    if ( n == 0 )
        return 1;
    else
        return ( n * factorial( n-1 ) );
}
```

1. Base Case

2. Pre-Process

3. Recursion

4. Post-Process



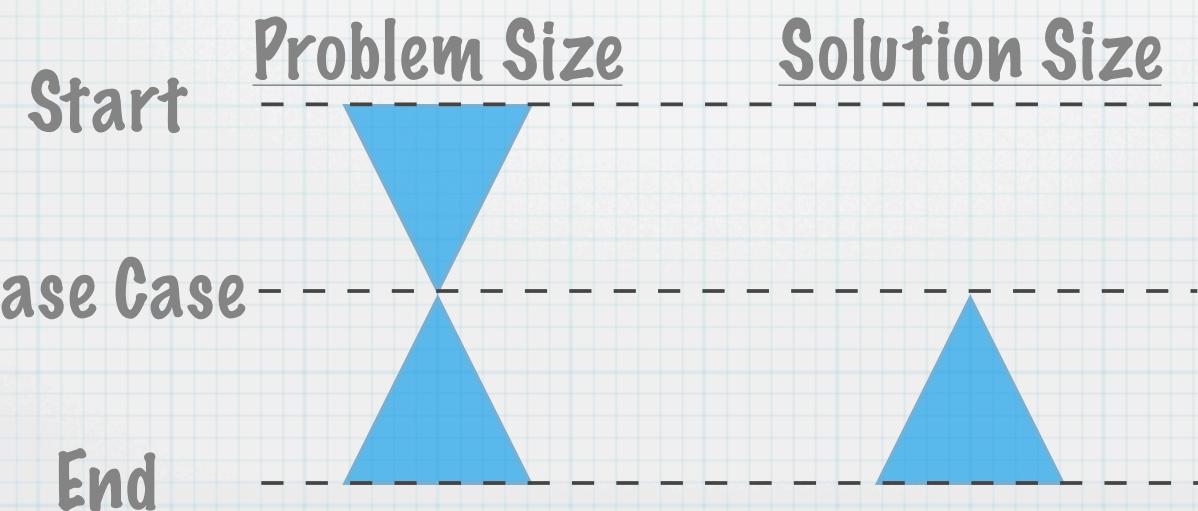
factorial(3)

$$\text{factorial}(3) = 3 * \text{factorial}(2) = 3 * 2 = 6$$

$$\text{factorial}(2) = 2 * \text{factorial}(1) = 2 * 1 = 2$$

$$\text{factorial}(1) = 1 * \text{factorial}(0) = 1 * 1 = 1$$

$$\text{factorial}(0) = 1$$



Tail Recursion

- * Style of recursive programming whereby the return value of the recursive call is not manipulated
- * Tail Recursion has no post-processing

Recursion Breakdown

```
static int fact_help( int n, int result )
{
    if ( n == 0 )
        return result;
    else
        return fact_help( n-1, n*result );
}

int fact_tail( int n )
{
    return fact_help( n, 1 );
}
```

Recursion Breakdown

```
static int fact_help( int n, int result )
{
    if ( n == 0 )
        return result;
    else
        return fact_help( n-1, n*result );
}

int fact_tail( int n )
{
    return fact_help( n, 1 );
}
```

1. Base Case

2. Pre-Process

3. Recursion

fact_tail(3)

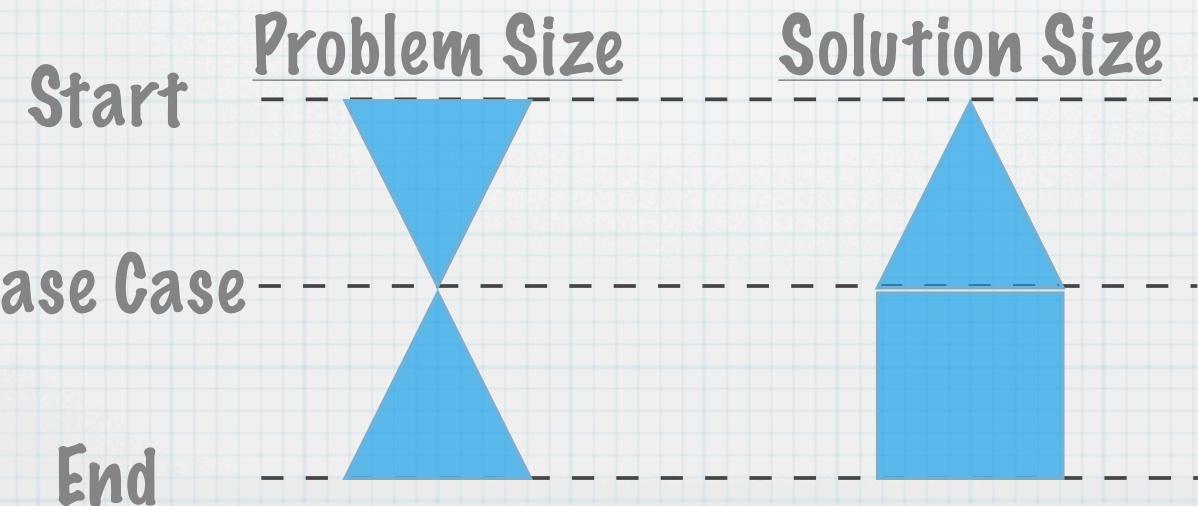
$$\text{fact_tail}(3) = \text{fact_help}(3, 1) = 6$$

$$\text{fact_help}(3, 1) = \text{fact_help}(2, 3) = 6$$

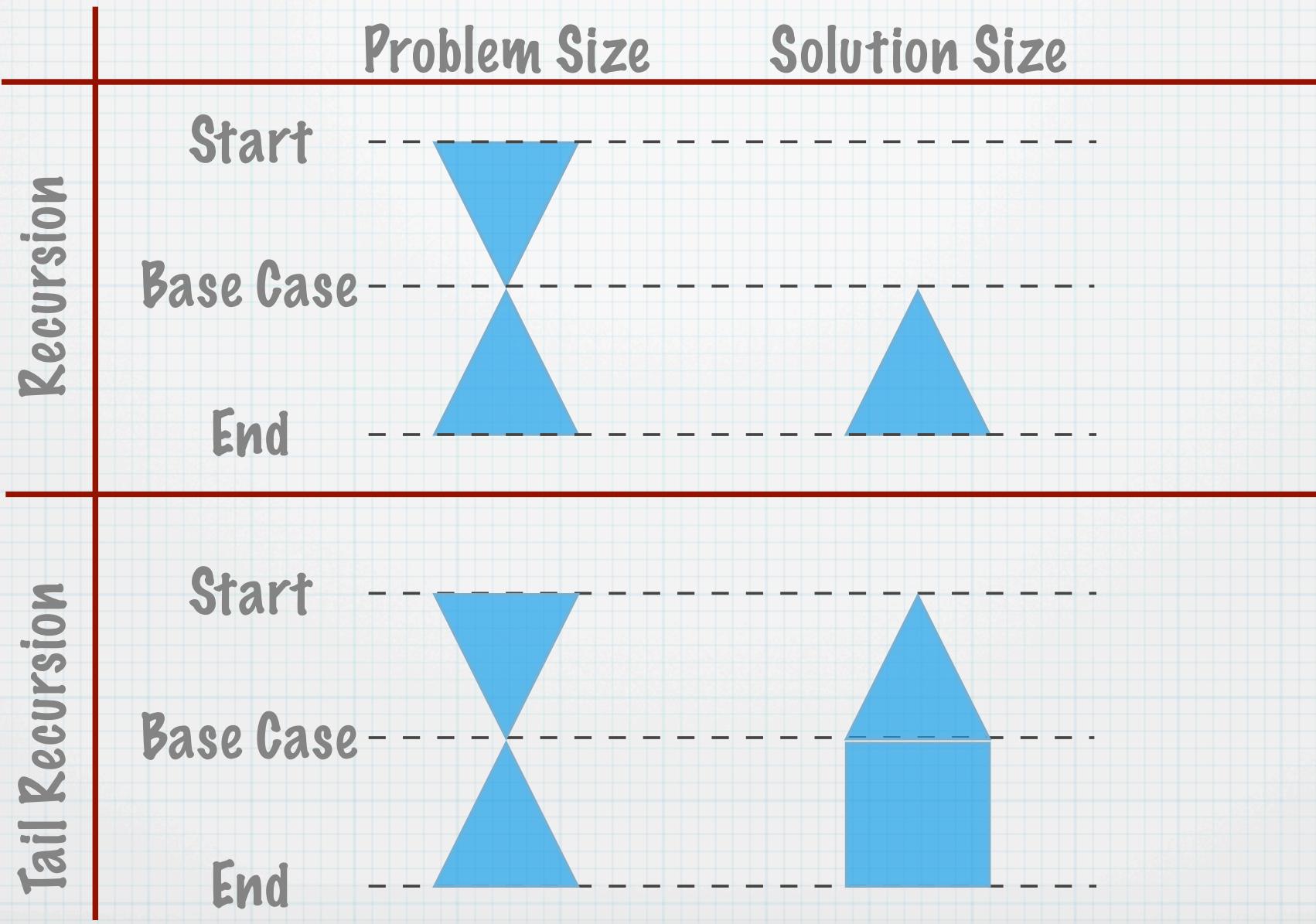
$$\text{fact_help}(2, 3) = \text{fact_help}(1, 6) = 6$$

$$\text{fact_help}(1, 6) = \text{fact_help}(0, 6) = 6$$

$$\text{fact_help}(0, 6) = 6$$



Recursion Comparison



Pin the Tail!

Consider recursive function foo, which of these statements are indicative of a tail recursive function?

- `return foo(x-1);`
- `return foo(x + foo(y));`
- `return foo(bar(x-1, y) + bar(x, y-1));`
- `return foo(x-1) + bar(y);`
- `return bar(y) + foo(x-1);`

List Example

```
list_t sum_piecewise( list_t x, list_t y )
    // REQUIRES: x and y are the same length
    // EFFECTS: returns the sum of lists x and y
{
    if ( list_isEmpty(x) )
        return list_make();

    return list_make( list_first(x) + list_first(y),
                    sum_piecewise( list_rest(x), list_rest(y) ) );
}
```

List Example - Tail

```
static list_t sum_piecewise_help( list_t x, list_t y, list_t result )
    // REQUIRES: x and y are the same length
    // EFFECTS: returns the sum of lists x and y
{
    if ( list_isEmpty(x) )
        return reverse( result );

    return sum_piecewise_help( list_rest(x), list_rest(y),
        list_make( list_first(x) + list_first(y), result ) );
}

list_t sum_piecewise_tail( list_t x, list_t y )
{
    return sum_piecewise_help( x, y, list_make() );
}
```

Outline

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- * Function Pointers

Code Reuse Discussion

- * Reasons NOT to copy-paste code:
 - * large code chunks can usually be extracted to functions
 - * variable conflicts in destination
 - * re-factoring difficulties

Motivating Example

Consider the following function:

```
int count_greater_than( list_t list, int n );  
// EFFECTS: returns the number of elements in list  
//           greater than n
```

What if we also wanted
count_less_than
count_prime
count_...

Function Pointers

Consider the following solution:

```
int count_predicate( list_t list, bool (*fn)(int) )
// EFFECTS: returns the number of elements in list
//           for which fn() returns true
{
    int counter = 0;

    while ( !list_isEmpty( list ) )
    {
        if ( fn( list_first( list ) ) )
            counter++;

        list = list_rest( list );
    }

    return counter;
}
```

Potential Predicates

```
bool is80s( int n )
{
    return ( ( n >= 80 ) && ( n <= 89 ) );
}

bool isEven( int n )
{
    return ( ( n % 2 ) == 0 );
}

bool lessThan100( int n )
{
    return ( n < 100 );
}
```

Final Thoughts

- * Assignment #2 due next Thursday
- * Work out functions by hand first
- * Give yourself time to think and sleep
- * Additional function pointer discussion will be available in discussion notes via CTools later this week